

quent than from the external callus. Most shoots arose from external callus produced by the pith and by the phloem, though in some cases the xylem and endodermis also were involved to a small extent. These regenerated shoots always established organic union with the vascular tissue of the decapitated shoot and became functional.

This observation of shoot regeneration by cabbage following treatment with Beta (3) indole-acetic acid is not an instance of induction of a new characteristic by a chemical agent. Occasionally (very rarely) decapitated control cabbage plants produced shoots without application of the acid. The chemical treatment apparently merely induces the internal conditions requisite for expression of a capacity which normally rarely comes to expression in the cabbage plant.

ETHEL GOLDBERG

DEPARTMENT OF BOTANY,  
UNIVERSITY OF CHICAGO

### EXACT PROBABILITIES IN CARD-MATCHING PROBLEMS

A DECK of  $mn$  playing-cards composed of  $m$  suits of  $n$  cards each, may be arranged in  $(mn)!/(n!)^m$  ways. If one of these is compared with some standard order, the number of coincidences is called the score. The frequency of any score  $r$  may be denoted by  $(r; m, n)$ . Huntington<sup>1</sup> gave the values of  $(r; 3, 3)$  and  $(r; 4, 4)$ . He considered the labor in the determination of  $(r;$

TABLE 1

		6 × 6							
Score		Frequency							
0 ...	4	165	949	769	769	961	828	425	
1 ...	28	996	446	742	915	700	420	640	
2 ...	98	700	744	213	619	952	591	700	
3 ...	218	864	808	829	456	293	367	200	
4 ...	355	341	281	078	962	422	086	175	
5 ...	450	116	094	274	568	927	912	160	
6 ...	462	909	014	435	100	202	332	336	
7 ...	397	123	967	735	823	016	052	640	
8 ...	289	793	784	100	001	073	868	710	
9 ...	182	524	670	735	530	786	230	560	
10 ...	100	344	596	349	272	804	505	000	
11 ...	48	575	943	371	163	005	793	504	
12 ...	20	851	099	196	639	140	076	850	
13 ...	7	980	545	109	018	220	394	400	
14 ...	2	735	656	277	729	448	992	400	
15 ...		842	844	533	954	374	188	000	
16 ...		234	038	576	801	926	712	520	
17 ...		58	693	462	370	532	698	400	
18 ...		13	313	942	477	144	955	600	
19 ...		2	734	372	820	642	421	600	
20 ...			508	679	897	516	240	400	
21 ...			85	715	584	272	352	800	
22 ...			13	076	448	757	088	400	
23 ...			1	804	316	455	605	600	
24 ...				224	849	404	787	850	
25 ...				25	255	852	293	600	
26 ...				2	550	498	318	360	
27 ...					230	827	143	200	
28 ...					18	656	661	150	
29 ...					1	339	048	800	
30 ...						85	377	840	
31 ...						4	709	664	
32 ...							243	135	
33 ...							8	640	
34 ...								540	
35 ...								0	
36 ...								1	
	2	670	177	736	637	149	247	308	800

5,5) to be prohibitive. Sterne<sup>2</sup> found the values of  $(21; 5, 5)$  up to  $(25; 5, 5)$  but knew of no way to determine these for smaller  $r$ . Greville<sup>3</sup> has recently found all values of  $(r; 5, 5)$ ; his solutions are correct, but involve much labor.

The problem is by no means as difficult as these papers imply. Macmahon<sup>4</sup> gave a direct method of attack by which Greville's results may be checked with about 12 hours of machine calculation. I have recently determined the values of  $(r; m, n)$  for all  $m$  and  $n$  less than 7 ( $m$  and  $n$  not being necessarily equal). The frequencies for the case in which both  $m$  and  $n$  are 6 are given in Table 1.

BANCROFT H. BROWN

DEPARTMENT OF MATHEMATICS  
AND ASTRONOMY,  
DARTMOUTH COLLEGE

<sup>1</sup> Huntington, *SCIENCE*, 86: 499-500.

<sup>2</sup> Sterne, *SCIENCE*, 86: 500-501.

<sup>3</sup> Greville, *Journal of Parapsychology*, March, 1938.

<sup>4</sup> Macmahon, *Combinatory Analysis*, Vol. 1, p. 99-112, Cambridge, 1915.

### BOOKS RECEIVED

- DARLING, F. FRASER. *Bird Flocks and the Breeding Cycle*. Pp. viii + 124. Cambridge University Press. Macmillan. \$1.75.
- HILL, M. A. and J. BURTON LINKER. *Introduction to College Mathematics*. Pp. xii + 373 + 93. 188 figures. Holt. \$2.40.
- HORVATH, A. A. *The Soybean Industry*. Pp. vi + 221. Chemical Publishing Company of New York.
- KELLEY, TRUMAN L. *The Kelley Statistical Tables*. Pp. 136. Macmillan. \$4.50.
- KILBY, CLINTON M. *Introduction to College Physics*. Second edition. Pp. ix + 398. 389 figures. Van Nostrand. \$3.25.
- KILLIP, ELLSWORTH P. *The American Species of Psephenidae*. Pp. 335-613. Field Museum. \$2.50.
- MASSEY, H. S. W. *Negative Ions; Cambridge Physical Tracts, No. 1*. Pp. xii + 105. 19 figures. Cambridge University Press. Macmillan. \$1.75.
- Scientific Reports of the Great Barrier Reef Expedition, 1928-29; Vol. V, No. 5*, by OSKAR CARLGRÉN, *Ceriantharia and Zoantharia*. Pp. 177-207. 34 figures. 1 plate; Vol. VI, No. 1, by ROBERT GURNEY, *The Larvae of the Decapod Crustacea Palaemonidae and Alpheidae*. Pp. 40. 265 figures. British Museum, London. 5/ each.
- Scientific Reports of the John Murray Expedition, 1933-34; Vol. II, No. 2*, by E. F. THOMPSON and H. CARY GILSON, *Chemical and Physical Investigations*. Pp. 15-81. 16 figures. 5/. Vol. V, No. 1, by H. G. STUBBINGS, *Phyllirhoidae*. Pp. 14. 5 figures. 2/. Vol. V, No. 5, by M. RAMADAN, *The Astacura and Palinura*. Pp. 123-145. 12 figures. 2/6. Vol. V, No. 6, by W. T. CALMAN, *Pycnogonida*. Pp. 147-166. 10 figures. 2/6. British Museum, London.
- SEAVEY, GEORGE. *Edward Wilson; Nature Lover*. Pp. xi + 221. Illustrated. Dutton. \$3.00.
- SMITH, ALPHEUS W. *The Elements of Physics*. Fourth edition. Pp. xix + 790. 789 figures. McGraw-Hill. \$3.75.
- TARR, W. A. *Introductory Economic Geology*. Second edition. Pp. xi + 645. 257 figures. McGraw-Hill. \$5.00.
- TIMM, JOHN A. *An Introduction to Chemistry*. Third edition. Pp. xvii + 568. 162 figures. McGraw-Hill. \$3.50.